

A DSP-based instrument for in-service wireless transmitter power measurement

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Abstract- A prototype of a DSP-based instrument for in-service transmitter power measurements is presented. The instrument implements a signal-selective algorithm for power measurements that is suitable for use in wireless environments, where possible uncontrolled interfering sources occupy the radio channel and are overlapped to the signal emitted by the transmitter under test, possibly in both time and frequency domains. The measurement method exploits the principles of cyclic spectral analysis, which are briefly recalled in the paper. Potentialities as well as use limitations for the prototype are discussed, also with reference to the results of some experimental tests.

I. Introduction

In-service testing of wireless transmitters is usually performed in the frequency domain and is potentially subject to the effects of interfering signals occupying the same channel or adjacent channels [1]-[2]. The problem is even more severe with regard to opportunistic systems that use Dynamic Spectrum Access (DSA), where the secondary user would temporarily occupy the spectrum unutilized by the primary user [3]-[4]. One of the key and easiest parameters that is measured during in-service transmitter testing is signal's power. Also, as highly integrated wireless communication circuits are often based on quadrature modulation, RF transmitter diagnostic is often based on I/Q impairment measurements, typically through loop-back tests [11],[12] or received signal processing [13],[14].

However, along with the well-known repeatability problems that power measurement on radiofrequency signals can suffer from [5], power measurements can actually become challenging when interfering signal(s) and useful signal overlap in time and frequency, especially in the case of low signal-to-noise (SNR) ratio [15],[16].

An innovative method to reliably measure signal power in presence of co-channel interference was presented in [6]. The method is based on a signal-selective algorithm that exploits cyclic spectral analysis [7] to measure the power of the sole desired signal, discarding interference. The cyclostationarity-based method exhibits good performance and succeeds in reliably measuring the desired signal's power even in cases when simple spectral analysis fails in separating desired and interfering signals.

The paper presents the prototype of a DSP-based instruments that, based on the aforementioned method, permits to perform in-service power measurements of wireless transmitters, even in unlicensed bands, where the risk of having uncontrolled interference is not negligible. In the following, after some basics on cyclostationarity, and theoretical information on the measurement principle, the prototype implementation is described and the results of some experiments are presented.

II. Wireless power measurements under interference

In this section, the proposed measurement method for in-service transmitter power measurements, which is suitable to operate in (critical) noise and interference conditions is presented. As the method is based on cyclic spectral analysis of the noisy signal, some notes on cyclostationarity are first given, for the sake of readability. Then, details on the measurement method are provided, along with a presentation of the cyclic spectral characteristics of the most common modulation formats, which are needed to implement the method.

A. General aspects of cyclic spectral analysis

A continuous-time real-valued stochastic process $x(t)$ is said to be almost-cyclostationary (ACS) in the wide sense if its autocorrelation function $R_x(t, \tau)$ is an almost periodic function of t . In such case, $R_x(t, \tau)$ can be expressed as the limit of a uniformly convergent sequence of trigonometric polynomials in t :

$$R_x(t, \tau) = \sum_{\alpha \in A} R_x^\alpha(\tau) e^{j2\pi\alpha t} \quad (1)$$

The coefficients of the sequence, $R_x^\alpha(\tau)$, are named *cyclic autocorrelation functions*, whereas α are the *cycle frequencies*. The vast majority of communications signals are ACS, as a consequence of a periodicity of some kind, connected with operations such as for instance coding, modulation or sampling. Their cycle frequencies are thus usually associated with typical parameters such as baud rate, sample rate and carrier frequency. When the autocorrelation function $R_x(t, \tau)$ is a periodic function of t (e.g. with period T), the set A contains cycle frequencies that are all multiple of a fundamental one (i.e. $A \equiv \left\{ \frac{n}{T} \right\}_{n \in \mathbb{Z}}$), and the process $x(t)$ is said to be cyclostationary in the wide sense.

A second-order characterization of ACS processes in the frequency domain can be easily obtained from (1):

$$E\{X(f_1)X^*(f_2)\} = \sum_{\alpha \in A} S_x^\alpha(f) \delta(f_2 - f_1 + \alpha) \quad (2)$$

where $X(f)$ is the Fourier transformation of $x(t)$, which is assumed to exist at least in the sense of distributions (generalized functions), with probability 1, $\delta(\cdot)$ is the Dirac delta, the superscript $*$ is the symbol of the operation of complex conjugation, and

$$S_x^\alpha(f) \triangleq \int_{\mathbb{R}} R_x^\alpha(\tau) e^{-j2\pi f \tau} dt \quad (3)$$

is usually referred to as either *cyclic spectrum* at cycle frequency α or *spectral correlation density function*.

Special care must be put when exploiting cyclic spectral analysis results to sampled signals. Indeed, it can be shown that the sampled version of a continuous-time almost-cyclostationary signal is a discrete-time almost-cyclostationary signal, whose cyclic spectra are related to those of the continuous-time signal [8]. However, aliasing can occur in the cyclic spectral domain, just as it can happen in the frequency domain. In this case, the avoidance of aliasing is granted by the choice of a sampling frequency that is as high as at least four times the bandwidth of $x(t)$, assuming $x(t)$ is a strictly band-limited process. A thorough and comprehensive treatment of cyclostationarity can be found in [7] and reference therein.

B. Power measurement

The measurement method implemented in the proposed DSP-based instrument was originally presented in [6]. It is based on a signal-selective algorithm that exploits the possibility of achieving signal separation in the cyclic spectral domain, even when in both the time and frequency domains signal and interference (plus noise) are completely overlapped. The basic idea is to extract the cyclic spectra of the original signal by processing the samples of the combination of signal and interference, and then to measure signal power thanks to a straightforward analytical relation between cyclic spectra and power. This is possible only if the analysis is conducted at a cycle frequency that is exhibited by the signal but not by interference. Please note that such assumption is not too limiting, as the condition under which signal and interference have coincident sets A (see equation (1)) is extremely rare.

Assuming the received signal $v(t)$ is the sum of the signal $x(t)$ and interference $y(t)$, if $x(t)$ and $y(t)$ are zero-mean and uncorrelated, then it holds

$$S_v^\alpha(f) = S_x^\alpha(f) + S_y^\alpha(f) \quad (4)$$

So, if the analysis is conducted for a value of α that is not a cycle frequency of the interference $y(t)$, which means $S_y^\alpha(f) = 0$, equation (4) reduces to

$$S_v^\alpha(f) = S_x^\alpha(f) \quad (5)$$

and the cyclic spectrum $S_x^\alpha(f)$ can thus be easily estimated from $v(t)$.

Now, considering a modulated signal $x(t)$

$$x(t) = s(t) \cos(2\pi f_c t + \varphi_0) \quad (6)$$

where $s(t)$ is a PAM (pulse amplitude modulated) signal with a wide-sense stationary and white modulating sequence, it can be shown [6] that $x(t)$ is ACS and its cycle frequencies are $\left\{\frac{k}{T_0}\right\}$ and $\left\{\pm 2f_c + \frac{k}{T_0}\right\}$, $k \in Z$.

If $x(t)$ is rewritten as $A x_1(t)$, where $x_1(t)$ is a unitary power signal, then from (5), the power of the signal $x(t)$, i.e. A^2 , can be obtained as

$$A^2 = \frac{\int_{-\infty}^{+\infty} |S_v^\alpha(f)| df}{\int_{-\infty}^{+\infty} |S_{x_1}^\alpha(f)| df} \quad (7)$$

where the cyclic spectrum of $x_1(t)$ depends on the transmitter and can be assumed to be known, since the cyclic spectra of the most common modulated signals are known [9].

III. Prototype of the instrument

The prototype of the instrument is shown in Fig. 1. It consists of an external 14-bit analog-to-digital converter (ADC) AD9244, characterized by 65 MS/S maximum sampling frequency, an extender that allows interconnection between the ADC and the digital signal processing unit, and an ADSP-21364 Sharc processor, mounted on a compatible development board by Analog Devices (EZKIT).

The ADSP Sharc processor is specifically addressed to real-time applications. In its architecture, three fundamental parts can be distinguished: the core processor, the memory block and the I/O processor. The core processor has two computational units and a cache memory to store frequently occurring instructions. Each computational unit has its own multiplier, ALU, shifter and data register file. The computational units are able to can execute for each cycle a sum, a multiplication and a dual data fetch. The system is able to operate in SIMD (single instruction multiple data) mode, when both computational units are used simultaneously. Memory access and data transfer is performed through a dedicated I/O processor, different from the core processor.

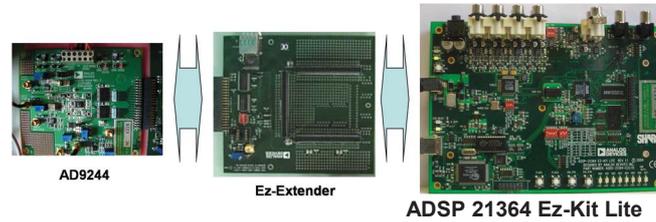


Figure 1. Instrument prototype

When a new power measurement is to be made, a boot thread is started to initialize the process. Specifically, it unmasks an interrupt request to give start to the data transfer from the ADC to the memory buffer of the processor.

After the digitization, which exploits all the memory depth, the samples are processed to estimate the cyclic autocorrelation function, which could in principle be calculated as

$$R_{xy}(m) = \begin{cases} \frac{1}{N} \sum_{n=0}^{N-m-1} x_{n+m} y_n^*, & m \geq 0 \\ R_{xy}^*(-m), & m < 0 \end{cases} \quad (8)$$

where $x_n = x(n T_s)$, $T_s = 1/f_s$ being the sampling period, and $y = x e^{-j2\pi a t}$. Actually, the vector y is memorized as a global variable so as to avoid a time-consuming recalculation for each value of m , and to comply with the memory limitation for local variables, the sum in (8) is calculated by exploiting the additive property, i.e. in four successive steps. Moreover, the operations are directly performed on the real and imaginary parts of the numbers in (8) in order to minimize the call to nested functions. Furthermore, to reduce the computational burden and consequently the measurement time, the autocorrelation is windowed, i.e. it is calculated only for the most relevant values of m .

Subsequently, the fast Fourier transform (FFT) algorithm is applied to the autocorrelation in order to straightforwardly estimate the cyclic spectrum. This is the reason why the autocorrelation is calculated on a number of points equal to a power of 2.

Finally, the power measurement is performed by summing the modulus values of the cyclic spectrum and dividing the result by a known scaling factor, i.e. making a discrete calculation of the right-side member of

expression (7).

IV. Experiments

Some experiments have been conducted to evaluate the performance of the prototype in emulated conditions, i.e. when interfering signals are digitally synthesized and summed to the samples of the useful signal. In these tests, channel conditions such as multipath and fading have not been taken into account. It is worth noting that the anti-aliasing conditions cited in the previous section, along with the limited sampling frequency of the prototype has forced to take into consideration signals at relatively low frequencies.

The measurement station is shown in Figure 2. It includes a 14-bit AWG Agilent Technologies E4438C, used to emit the PAM signal as well as the interfering signals, and a digital processing and control unit, i.e. a laptop, which are interconnected through a standard IEEE 488 interface bus. The prototype is connected to the laptop and controlled through a USB cable.

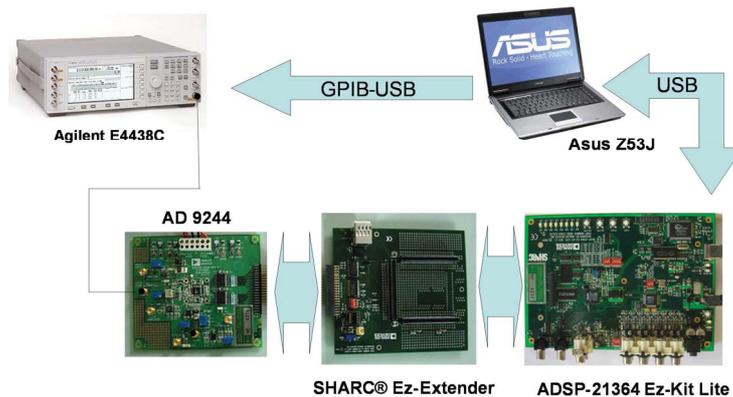


Figure 2. Measurement station.

To evaluate the quality of the power measurement results, a number of initial tests have been conducted on the sole signal, when no interference is added. In all the tests, the difference between the measured power value and the nominal power value is calculated for different cycle frequencies, and the histogram of the differences is evaluated. This permits to compare the ability of the instrument to extract the power of the useful signal even in critical interference conditions and to compare the repeatability of such measurements to the “intrinsic” repeatability exhibited in absence of interference.

The signal generated for the tests is a binary PAM with root-raised cosine base pulse, whereas PAM and multitone signals have been considered as interfering signals.

Table 1 shows the achieved results, in terms of average and maximum difference Δ , and of standard deviation σ , over two hundred repeated measurements for each cycle frequency considered, for a PAM signal characterized by a symbol rate $T = 200 \mu\text{s}$, and a carrier frequency $f_c = 10 \text{ MHz}$. Differences and standard deviations are expressed in percentage relative terms with respect to the nominal power value.

Table 2 and Table 3 show, respectively, the results obtained with multitone and different PAM interfering signals, the useful signal being the same. In particular, the multitone interference is the superposition of two sinusoids at frequencies 8.5 MHz and 9.5 MHz. It is no surprise that if the measurement is performed at cycle frequencies $2f_c$ and $1/T + 2f_c$, the results are very poor: this happens because the interfering signals exhibits cyclostationarity at frequencies 17 MHz and 19 MHz, which are pretty near $2f_c$ and $1/T + 2f_c$. As stated in the previous section, the analysis has to be carried out at cycle frequencies that are not common to the useful signal and the interference. At the same time, results achieved with $\alpha = 1/T$ are comparable to those obtained without interference.

Table 1. Measurement results without interference.

Cycle frequency	Average Δ [%]	Maximum Δ [%]	Std. dev. σ [%]
1/T	0.8	10	2.0
2f _c	2.2	7.7	2.4
1/T + 2f _c	5.7	13	2.4

Table 2. Measurement results with multitone interference.

Cycle frequency	Average Δ [%]	Maximum Δ [%]	Std. dev. σ [%]
1/T	2.8	5.1	2.1
2f _c	20	30	7.5
1/T + 2f _c	12	16	4.5

As regards interfering signals sharing the same modulation format as the useful signal (i.e., PAM), results shown in Table 3 give evidence of the good performance of the method implemented on the prototype, since the values of average percentage difference and standard deviation are generally comparable to those achieved without interference, and reported in Table 1. It can again be noted that choosing a cycle frequency that is exhibited also by the interfering signal for the analysis brings to very bad results due to the impossibility of separating the cyclic spectra of useful signal and interference.

Table 3. Measurement results with PAM interference.

Cycle frequency	<i>PAM interference with the same T</i>			<i>PAM interference with the same f_c</i>		
	Average Δ [%]	Maximum Δ [%]	Std. dev. σ [%]	Average Δ [%]	Maximum Δ [%]	Std. dev. σ [%]
1/T	95	99	3.4	2.2	6.1	2.2
2f _c	3.0	4.2	1.6	83	98	2.7
1/T + 2f _c	3.9	5.9	2.8	5.3	10.5	2.5

V. Conclusions

The paper has presented the prototype of a DSP-based instrument for in-service transmitter power measurements, based on a signal-selective algorithm that exploits the principles of cyclic spectral analysis. To be used effectively, the method requires the a priori knowledge of the basic parameters of the transmitted signal, such as the modulation format, the symbol rate and the carrier frequency, and requires that the signal emitted by the transmitter under test and possible interfering source do not share at least one cycle frequency.

In spite of the efforts to optimize the hardware resources available for the prototype, it still suffers from some limitations, mainly connected with the maximum sampling frequency and memory depth and has therefore to be considered as a proof of concept for possible application to radiofrequency transmitter. However, the experimental results presented have proven that the proposed method, which was originally presented in [6], exhibits good performance on real communication signals.

Ongoing research activities are mainly focused on the introduction of a down-conversion section before the digitization, which can make the use of the same DSP prototype feasible for signals at higher frequencies. An interesting alternative could be the adoption of band-pass strategies like in [17] and [18], with suitable adaptation to cope with the further constraints that have to be introduced to avoid cyclic aliasing.

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