

Accuracy and precision studies for range-only underwater target tracking in shallow waters

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Abstract – This paper provides a study on the precision, and the accuracy, of an underwater target tracking system with acoustic waves, using range-only and single-beacon methods, in shallow waters environments. For this study, different field tests have been realized in the OBSEA test site, a well-known and monitored area at 4 km from the coast and at 20 meters of depth, in the Mediterranean Sea (Barcelona). The tests have been conducted using two acoustic underwater modems from the company LinkQuest Inc. Moreover, the autonomous underwater vehicle developed by the *Universitat Politècnica de Catalunya* (called Guanay II) have also used to perform the tests.

Keywords – Range-only, single-beacon, underwater target tracking, position accuracy, position precision, autonomous vehicle, and AUV.

I. INTRODUCTION

Range-only and single-beacon architecture for underwater acoustic target tracking using autonomous vehicles has numerous advantages, such as low deployment complexity, and the possibility to cover large areas. On the other hand, this method can also be integrated in multi-vehicle collaborations, which opens new possibilities for ocean exploration. For these reasons different studies have been conducted during the last years [1].

However, due the complexity of the underwater acoustic channel communications, and the complexity to have a standard underwater positioning system, different aspects of this method are still open. For example, the precision and accuracy that can be achieved in shallow waters, which can also be altered for the specific bathymetry of the area.

Previous works that we have conducted recently, [2] and [3], have shown that the specific shallow water environment can cause an important impact in the range error, and therefore, in the accuracy and precision of target

localization. As it is well known, the main issue brought by shallow waters environment is the multi-path effect, which can cause important errors in range measurements.

The ranges between two points are usually measured using two acoustic modems. One installed in the target and another one in the vehicle. Typically, these modems have a standard command to know the distances between them using a two-way message exchange. Where the range can be derived easily knowing the Time of Flight (TOF) of the message and the sound velocity in water (approximately 1500 m/s).

However, the exact sound velocity is usually difficult to know, due its sensitivity in front of temperature or salinity variations. This can cause a systematic error in range measurements, and therefore, reduce the accuracy of the target estimation. Moreover, some outliers in range measurements can also be produced through the multipath effect, which introduce a non-Gaussian error in range measurements.

The aim of this paper is to study and characterize the best accuracy and precision that can be reached in shallow water scenarios, using range-only and single-beacon target tracking algorithms. For this propose, different tests have been conducted, and different algorithms have been compared such as, Least Square (LS), Extended Kalman Filter (EKF) and Particle Filters (PF).

In this paper, the definitions of accuracy and precision from the Joint Committee for Guides in Metrology (JCGM) [4] are considered, where the accuracy is defined as the closeness of agreement between a measured quantity value and a true quantity value, and the precision as the closeness of agreement between measured quantity values obtained by replicate measurements.

The complexity of the water channel is well known [5], which introduces different sources of errors in acoustic positioning systems. The main sources of error were explained in our previous work [3].

The multipath effect is the most important one in shallow water environments [6-7], as it was also observed

in [3], which can introduce a non-Gaussian noise error and different outlier points [8]. These problems have an important implication in the accuracy and precision of target positioning, especially when the range-only single-beacon method is used.

In this paper, we want to study these issues in our specific scenario, the OBSEA test site in Barcelona, with the main goal of localize and track and underwater target using an Autonomous Underwater Vehicle (AUV), and range-only and single-beacon techniques.

II. DESCRIPTION OF THE METHOD

The main architecture behind the range-only and single-beacon underwater target tracking using autonomous vehicles is shown in Fig. 1. The idea is to estimate the position of an underwater target with a known depth, using only the ranges between the target and an autonomous vehicle, which is in a known position. The autonomous vehicle can be a surface vehicle with a GPS, or an underwater vehicle with a good dead-reckoning system. In our study, the vehicle tested is an AUV used as a surface unmanned vehicle called Guanay II that has been developed by *Universitat Politècnica de Catalunya* (UPC), and it is called Guanay II [9]. This vehicle is equipped with a GPS, and an acoustic modem configured as a master.

On the other hand, the underwater target is a second modem, deployed on the water at 5 meters of depth using a buoy, with known GPS position. This modem is used as a slave.

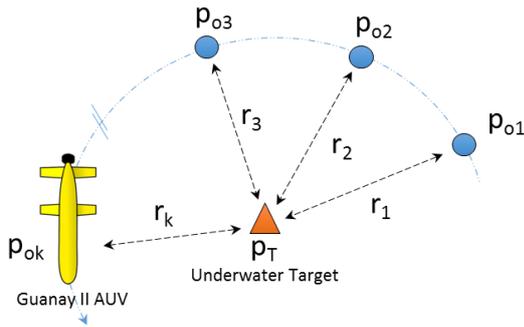


Fig. 1. Representation of the Guanay II (as observer) and the underwater Target

With this configuration, and using the LS, EKF and PF algorithms, a comparative study have been done. These three algorithms are well known and in this paper only the main aspects are presented. If a detailed information is needed, please see the work done in [10-12], and the references therein.

A. Least Square algorithm (LS)

The LS algorithm was used in our previous work [2], where this algorithm was developed to compute the

location of a static underwater target using only the range measurements

$$\bar{r}_k = \|\mathbf{p}_T - \mathbf{p}_{ok}\| + w_k, \quad k \in \{1, 2, \dots, m\} \quad (1)$$

where $\mathbf{p}_T = [x_T \ y_T]$ and $\mathbf{p}_{ok} = [x_{ok} \ y_{ok}]$ are the target and the AUV positions at time step k , with some zero mean Gaussian measurement error $w_k \sim \mathcal{N}(0, \sigma^2)$, where σ^2 is its variance.

The main idea of this method is to linearize the system using the squared range measurements. Then, the target position can be computed using different AUV positions, and triangulation techniques.

B. Extended Kalman Filter (EKF)

The EKF algorithm is used to estimate the state vector of a wide variety of non-linear problems. For underwater target tracking using range-only methods, the EKF main parameters are shown below. Firstly, we have the state vector

$$\mathbf{x}_k = [x_{Tk} \ \dot{x}_{Tk} \ y_{Tk} \ \dot{y}_{Tk}]^T \quad (2)$$

where x_{Tk} and y_{Tk} are the target position, and \dot{x}_{Tk} and \dot{y}_{Tk} are their velocities, at time step k . Then, we have the motion model

$$\mathbf{x}_k = \mathbf{F}_{k-1} \mathbf{x}_{k-1} + \mathbf{Q}_{k-1} \quad (3)$$

where \mathbf{F}_k is the state transition matrix, and \mathbf{Q}_k is the process noise respectively at step k . Finally, the measurement model is:

$$h(\mathbf{x}_k) = \sqrt{(x_{Tk} - x_{ok})^2 + (y_{Tk} - y_{ok})^2} + w_k \quad (4)$$

where x_{ok} and y_{ok} are the AUV (as an observer) easting and northing positions at each time step k .

C. Particle Filter (PF)

The main idea behind PF [14] is the use of grids to represent the spatial state, and a posterior computation over these grids recursively. This method has the capability of solving nonlinear estimation problems with a multimodal posterior probability distribution function.

The PF uses the same state vector, motion and measurement models of the EKF to represent each particle of the filter. Moreover, each particle has an associated importance weight

$$W_k^n = p(z_k | \hat{\mathbf{x}}_k^n) \quad (5)$$

which is related to the measurement z_k . And a resampling step which generate a set of new particles from the previous set, according to the importance weights calculated.

III. TEST SETUP DESCRIPTION

Several field tests have been conducted in the underwater cabled observatory OBSEA [13], in Barcelona, in order to compare filter’s performance. This observatory is at 4 km from the coast, and in a shallow water environment (20 meters of depth).

Although the algorithms explained above was designed for tracking a moving target, a preliminary test have been done to observe its performance in a static scenario, which can be observed as an initialization point for the dynamic scenario. Therefore, this is an important point to study, which will have an important effect, not only for static targets, but also for moving targets. The tests conducted in the OBSEA to study this performance were designed as follows.

One linkQuest Inc. modem was deployed on the one hand on the OBSEA’s buoy and attached at 5 meters of depth, on the other hand a second modem was installed in the Guanay II AUV, as described in Fig. 2. The first modem was used as a slave, which only responded the synchronization commands sent by the master modem, fixed on the AUV.

The path designed for this test was two pentagon lines around the target, which had respectively 100 meters and 200 meters of radius for first and the second experiment (see Fig. 2). During this path, the AUV was constantly measuring the ranges between the target and himself, with a period of 30 seconds, approximately. The best path to break the system’s ambiguity is a circle. However, since the AUV’s navigation system is not optimized to do such kind of trajectories, we chosen a pentagon trajectory which is closed enough to a circle shape.

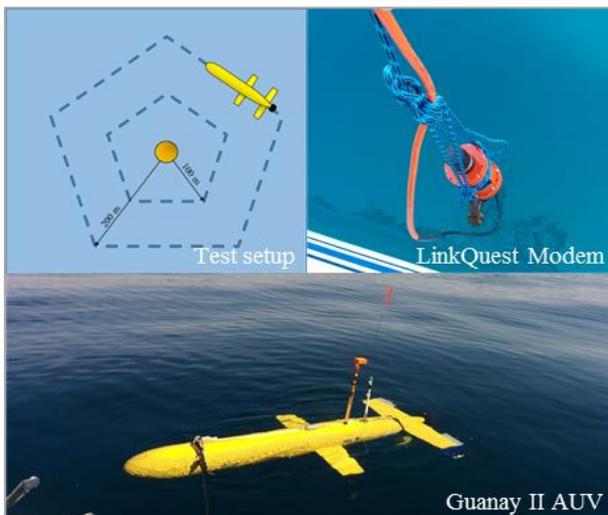


Fig. 2. Upper left: test setup with target position (orange circle), and Guanay II trajectories, pentagons with 100 m and 200 m of radius. Upper right: picture of one of the LinkQuest Inc. acoustic modems used for the test. Lower picture: Guanay II during the mission.

IV. RESULTS AND DISCUSSIONS

The path done by our AUV during the test can be observed in Fig. 3, where the big blue circles are the waypoints (WP) of the path, the small blue circles are the true path completed and also indicates when the AUV obtained a new range, and the red triangle is the true target position. Moreover, the black start and circle indicate the start point, and the end point, respectively.

We can see that Guanay II started at 50 meters from the target and then it did a first pentagon, then went to the centre and started the second and biggest pentagon. During all this path, the AUV acquired 83 ranges between himself and the target position.

Several simulations have been performed, using the same GPS positions as Guanay II acquired during the test, but with an ideal group of ranges instead of the acquired ones. This allows us to simulate different scenarios with different noise levels in order to study the performance of the algorithms.

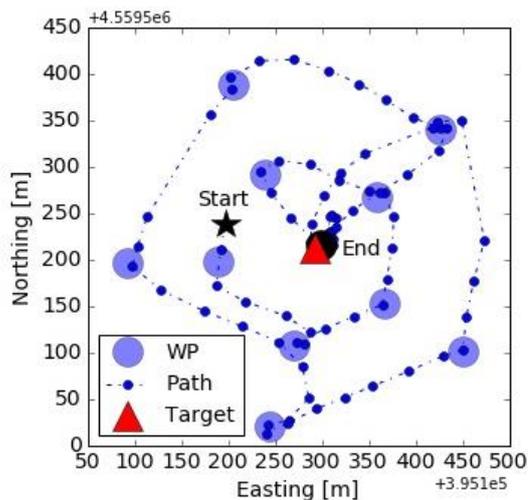


Fig. 3. Guanay II trajectory during the field test (blue dots). Moreover, we can observe the initial and final position (black start and dot respectively), the waypoints which indicated the path (big blue dots), and, finally, the true target position (red triangle).

A. Simulations with true GPS positions

To study de boundaries of the three algorithms (LS, EKF and PF), we have run them under three different environment conditions, using the true GPS positions obtained during the field test, and ideal ranges with simulated noise levels: a low-noise scenario (a Gaussian noise with a Standard Deviation (STD) equal to 1 meters), a medium-noise scenario (with a STD equal to 2 meters), and a high-noise scenario (with a STD equal to 4 meters).

As an example, we have taken the medium-noise scenario, and we have run it 100 times to observe the filters response variability, and the Root Mean Square Error (RMSE) as a function of time, or equivalently, as a function of each new range introduced in the filters. This

can be observed on Fig. 4, where we highlight the mean of the RMSE after 100 iterations (dark line) and its standard deviation (light coloured areas). The setting time T_s is computed when the error is below the dotted line configured at 20 m.

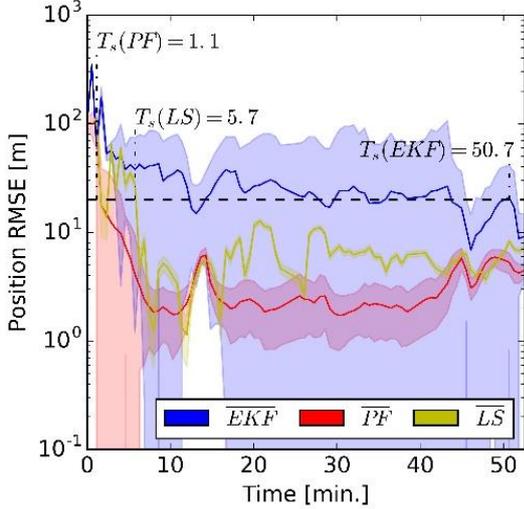


Fig. 4. Target position error versus time, or new range. Dark line is the mean after 100 iterations, and light coloured area is its STD. For a Gaussian noise of 0m of mean and 2 m of STD.

We can observe that the EKF has the worst performance, which means that it is very sensitive to the noise, and therefore leads to difficulties to estimate the true target position. An error lower than 20 meters is reached after almost 51 minutes which is definitely too much for target tracking purposes. On the other hand, both PF and LS algorithms have much better performance with a setting time of 1.1 and 5.7 minutes, respectively.

Finally, on Fig. 5 a better representation of the algorithms' accuracy and precision are carried out, where each scenario has been iterated 100 times. The graphs show the last 10 filter's estimations for each iteration

leading to a total of 1000 points (small dots). Moreover, the ellipses show the covariance matrix of each dataset in two dimensions. This covariance represents a 2D standard deviation of the estimations with a 95.45% of confidence interval. The main points to notice on Fig. 5 are the following:

Least Square algorithm (LS): we can see that the LS algorithm has the lowest noise influence with a high precision, however its accuracy is not as good as its precision. It leads to a STD of 0.26 m and 1.42 m, on its axis, and a bias error of 5.94 m (for 1 m of noise).

Particle Filter (PF): the PF has a quite good performance in low and medium noisy scenarios with high precision and higher accuracy than LS. It leads to a STD of 0.85 m and 1.61 m, on its axis, and a bias error of 4.68 m (for 1 m of noise). This indicates a good robustness against ranging noise. However in higher levels of noise, its prediction becomes worst

Extended Kalman Filter (EKF): this algorithm is shown to be the most vulnerable against ranging noise, as observed also previously. Whereas its precision is really poor, it leads to a good accuracy. It provides a STD of 4.95 m and 7.65 m, on its axis, and a bias error of 0.83 m (for 1 m of noise).

All these parameters are summarised in Table 1.

B. Comparison between simulations and field test

After the simulations described above, the experimental ranging error have been studied in order to obtain its statistics. With this information, the simulation results, and the real result obtained during the test, can be fairly compared. This allow us to validate the mathematical formulation, and the algorithms.

The ranges errors obtained during the test are shown on Fig. 6. Moreover, the associated histogram can be observed on Fig. 7, where we can see that the error has a Gaussian shape distribution with -0.22 m of mean and 2.59 m of STD

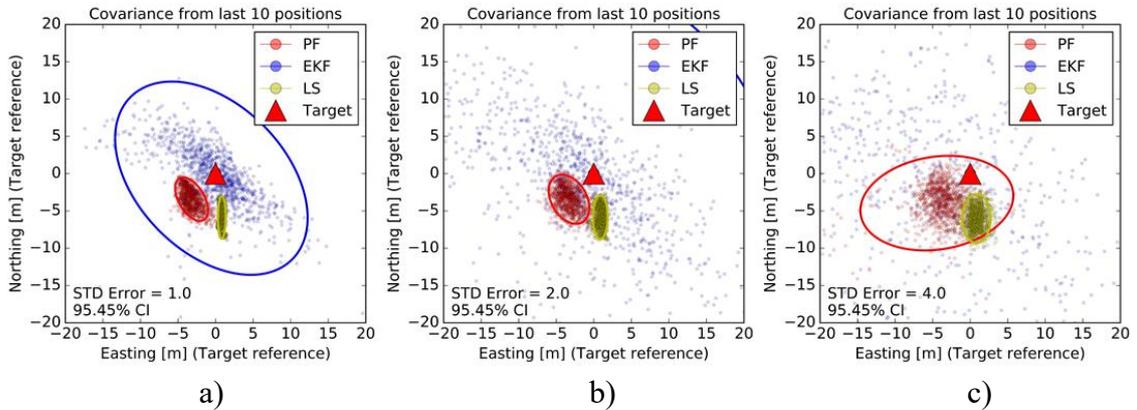


Fig. 5. Representation of the algorithms' covariance error in three scenarios: low-noise (a), middle-noise (b) and high-noise levels (c), which have a STD of 1 m, 2 m, and 3 m respectively. These values have been obtained with a simulation 100 iterated, and using the last 10 estimations of each iteration.

Finally, the target position estimations obtained during the OBSEA test are shown in Fig. 8, where last 10 estimations of the filters are represented. We also add on the figure the error covariance as done previously (elliptic lines). These results can be compared with the simulation work done in section A to see its correlation.

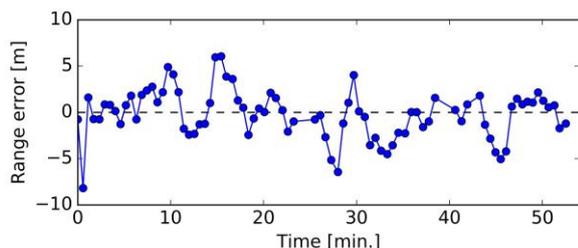


Fig. 6. Range error obtained during the OBSEA test.

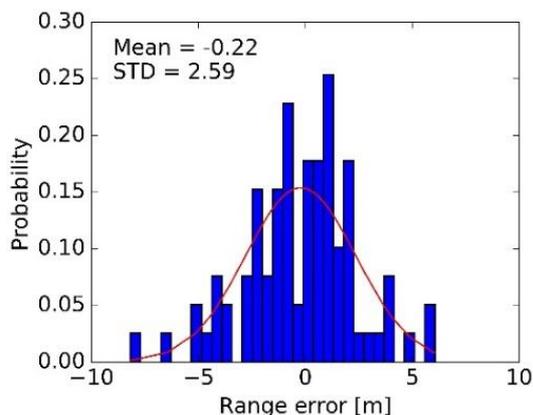


Fig. 7. Range error histogram obtained during the OBSEA test, which have an error mean of -0.22 meters and a Standard Deviation (STD) of 2.59 meters.

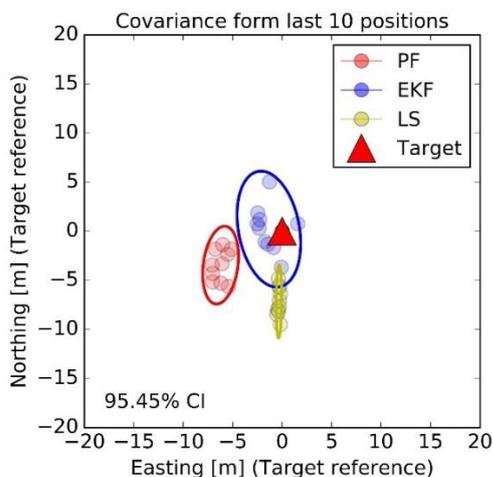


Fig. 8. Representation of the last 10 target estimations during the OBSEA test, using the PF, EKF and LS algorithms. Ellipse circumference shows the point's covariance.

Table 1. Standard deviation and mean error of a target position estimation using LS, EKF, and PF algorithms, in three different noise scenarios (simulated). Values in meters.

	Noise level	STD of vector 1	STD of vector 2	Mean
PF	1	0.85	1.61	4.68
PF	2	1.17	1.78	4.76
PF	4	5.13	3.11	5.94
EKF	1	4.95	7.65	0.83
EKF	2	13.87	15.89	5.21
EKF	4	23.68	23.21	17.9
LS	1	0.26	1.42	5.94
LS	2	0.49	1.47	5.91
LS	4	0.94	1.63	6.09

V. CONCLUSIONS

Range-only and single-beacon method for underwater target localization and tracking is interesting for its low complexity deployment, and can be used in a wide ocean area. In this paper we have considered 3 algorithms namely Least Square (LS), Extended Kalman Filter (EKF), and Particle Filter (PF) methods and studied their accuracy and precision on simulation and field tests. We have observed both PF and LS methods have a higher robustness on ranging error than EKF approach. However, although PF and LS algorithms lead to high with a small standard deviations between estimations, they suffer from some bias, that should be compensated to obtain a better accuracy.

As a future work, these algorithm are going to be tested with a moving target instead of a static one, and more field tests will be carried out in order to study other aspects such as speed rate and setting time.

VI. ACKNOWLEDGMENT

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